

# A SMALL TURBOJET ENGINE MPM-20 WITH VARIABLE EXHAUST NOZZLE

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The aim of this thesis is to describe the jet engine MPM-20 with a variable nozzle exit, as a system with two degrees of freedom. The paper describes the development and current status of MPM-20 engine in the test engine. In the following analysis, in describing the effect of changing the nozzle exit section to run the engine with regard to the planned structural remodeling MPM20 engine. The core work is to address proposals for changes in the output control section. In the last part of this work is described showing the effect on the measurement speed due to changes in engine output variable exhaust nozzle section.

Key words. MPM-20, variable exhaust nozzle, exit face nozzle, LTKM, servo

## 1 INTRODUCTION

The object of the investigation and resolution of this work, is the air turbo trigger TS-20, modified for small jet engine MPM-20 and is located in a laboratory at the Faculty of Aviation Technical University in Košice. The engine, despite its size, different from other major engines of similar design. The engine of this class is suitable for laboratory experiments, because of its size and uncomplicated and the economic availability.

Plans to renovate the engine MPM-20 motor with adjustable output nozzle created a requirement for design control and review of the outlet nozzle of behavior to the use of such a system, which will be expanded to the second degree of freedom, whereas the first stage deals with the supply of fuel into the main combustion chamber.

The purpose of this thesis was to design the drive to change the outlet nozzle exit section and perform mathematical model that shows what effect a change in the output section MPM-20.

Controlling the nozzle exit area  $A_5$  is most often used to:

- Shortening the time required to start and the engine,
- To short the period of acceleration at maximum speed,
- To achieve the lowest fuel consumption
- To obtain maximum thrust.

## 2 SINGLEJET AND SINGLEROTOR AIR JET ENGINE WITH VARIABLE NOZZLE AS A CONTROLLED OBJECT

The purpose of the system output of air jet engine is to exhaust gases from the engine into the atmosphere, to guide them in the desired direction and simultaneously converts thermal energy and pressure of gas at the gas kinetic energy. The output tract thus obtained thrust force  $F$  that drives the aircraft forward.

Air jet engine in many cases uses a variable nozzle exit, which allows you to change the output nozzle critical section  $A_5$ .

Change of the section  $A_5$  size affects the total gas pressure in the turbine  $p_{4C}$ . In terms of joint work of the engine and turbo outlet nozzle that at a magnification of section  $A_5$ ,  $p_{4C}$  gas pressure decreases as the turbine. The total expansion pressure drop in gas turbine  $\pi_{TC}$  applies:

$$\pi_{TC} = \frac{p_{3C}}{p_{4C}},$$

where:  $p_{3C}$  - total gas pressure before the turbine,  
 $p_{4C}$  - total pressure of the gas behind the turbine.

Change  $A_5$  affects the value of  $p_{4C}$ , which compared to  $p_{3C}$  value changes significantly. This has the effect of maximizing up  $A_5$  the  $\pi_{TC}$  turbine pressure drop increases and vice minimize  $A_5$  reducing the pressure drop across the turbine  $\pi_{TC}$ . Work of turbine  $W_{TC}$  singlejet, shingleshaft aviation turbo engine determined by:

$$W_{TC} = c_{p,pl} \cdot T_{3c} \left[ 1 - \frac{1}{\frac{\kappa'-1}{\pi_{TC}^{\frac{\kappa'}{\kappa'}}}} \right] \cdot \eta_{TC}$$

Where:  $c_{p,pl}$  - specific heat capacity of gas at constant tension,  
 $T_{3c}$  - total temperature of the gas before gas turbine,  
 $\kappa'$  - poisson's gas constant,  
 $\eta_{TC}$  - total turbine efficiency.

According to the relation specific,  $W_{TC}$  turbine work is directly related to  $\pi_{TC}$ , and that depends on the  $A_5$ . This relationship explains the impact of controlling the nozzle exit section of the engine run. Change of  $W_{TC}$  has an impact on the value of the parameters of thermal circulation of engine engine as thrust  $F$  and specific consumption  $c_m$ .

The steady operation of the engine must be accomplished the condition:

$$W_{TC} \cdot \eta_m = W_{Kc}$$

Where:  $W_{TC}$  - total turbine work,  
 $\eta_m$  - engine mechanical efficiency,  
 $W_{Kc}$  - total compressor work.

The above conditions shows that:

- Engine will accelerate if the total work of the turbine  $W_{TC}$  increases:

$$W_{TC} \cdot \eta_m > W_{Kc}$$

- The engine will decelerate if the total work of the turbine  $W_{TC}$  reduces:

$$W_{TC} \cdot \eta_m < W_{Kc}$$

The introduction of variable cross section  $A_5$  is obtained in addition to the fuel mass flow  $Q_p$  into the main combustion chamber further regulatory parameter. Air jet engine becomes the object of regulation with two degrees of freedom.

### 3 ANALYSIS OF CONTROL THE OUTLET NOZZLES WITH VARIABLE GEOMETRY

For design of control, I came out from the basic entry requirements:

- The force required to control min. - 40 kg
- Railway leverage needed to change the section of the  $A_5$  min to  $A_5$  max - 40 mm
- Time to change cross - 1 sec.



Fig. 1 Output control system for MPM20 engine with variable output section

The force needed to control the is not the exact value, but only estimated, because, there is no technical documentation for the output system. In consultation with the leader of this thesis, gave me two available engines, for which I could design the control of the outlet nozzle. As the first, is electric motor, which output movement is a sliding movement and his name is MP-100M. As second option, with which I can work with, I was given HV DS8921 servo motor.

#### 3.1 Control using servo HV DS8921

Servo motor HV DS8921 is actually a miniature electric motor with gearbox.

Parameters:

- Torque up to 36.5 Nm kg.cm = 3.569 at 8.5 V,
- Maximum speed of rotation of 60° / 0.13sec.,
- Supply voltage range  $U = 6.0$  V to 8.5 V.



Fig. 2 Servo HV DS8921

On the positive side of this servo is that it provides the possibility of positioning the rotary shaft, and the output shaft position feedback member is sensed (usually a potentiometer) that transmits location data back to the built-in controller in servo. The electronics ensures the control of speed, direction of rotation of motor.

Desired location of output shaft is awarded to the control electronics as a pulse as width modulated signal as also known as PWM (pulse-width modulated) signal Fig 3.

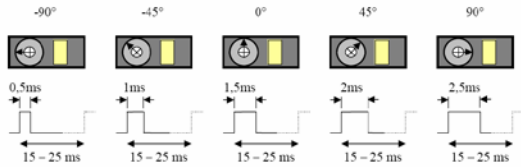


Fig. 3 Adjusting of Servo shaft position

In the design of the controlling the outlet nozzle by servo i take into consideration it's outputs to requirements that were imposed by output deck.

After several calculations, I excluded control servo by lever because the output of the multiplier lever mechanism to control the outlet nozzle I was always wrong and the ratio of force displacement. When sufficient deflection, there was very little force.

After further reflection it occurred to me to fit servo, with small cog gear, which will drive the large cog gear. Large cog gear would be directly linked to the deck through the output rod.

During the design of this control was predicted, that the force required to operate system will output will be maximum of 20 kg.

After implementation of the calculation, I found out, that control would be realistic and I realized it.

The output shaft of the servo, was planted by small cog gear whose diameter is  $d_p = 30$  mm, the radius  $r_1 = 15$  mm.

As a second cog gear used to pitch diameter  $d_p = 180$  mm, radius  $r_2 = 90$  mm.

On this combination of gearing and gear ratio  $i = 6$ , I computed the rotation of the small cog gear by  $\beta_1 = 174^\circ$ , the large sprocket is rotated by an angle  $\beta_2 = 29^\circ$ .

Point of links with a large cog gear with rod is on radius  $r_3 = 80$  mm. The strength of the rod would be  $F_3' = 259.17$  N - 26.4 kg.

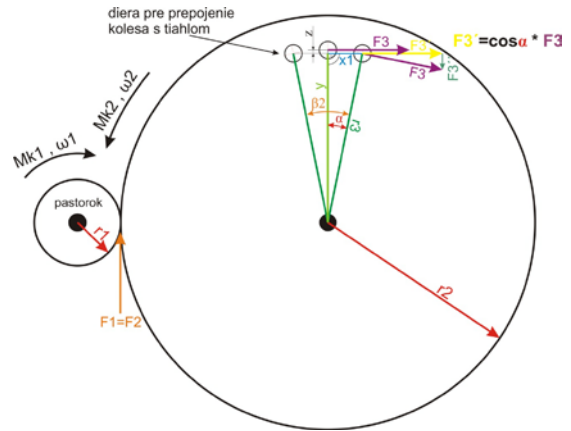


Fig. 4 Graphical outline of the calculation

From the Picture can be seen that small cog gear would its strength (whose size is determined from the torque of the servo  $Mk_1$ ) transferred to the large cog gear on a pitch circle. Thus  $F_1 = F_2$  and it is known that:

$$- Mk_1 = 3.569 \text{ Nm}$$

$$- r_1 = 15 \text{ mm}$$

Then:

$$Mk_1 = F_1 \cdot r_1$$

$$F_1 = F_2 = \frac{Mk_1}{r_1}$$

To find the value of  $F_3$  will apply:

$$Mk_2 = Mk_3$$

$$F_2 \cdot r_2 = F_3 \cdot r_3$$

$$F_3 = \frac{F_2 \cdot r_2}{r_3}$$

Using the trigonometric sinus function, we can calculate the angle  $\alpha$ .

$$\sin \alpha = \frac{r_3}{x_1}$$

The angle  $\alpha$  is only for the value of  $x_1$  which is  $\frac{1}{2}$  of the required movement length.

After obtaining the value of angle  $\alpha$ , we can calculate the value of  $F_3'$ .

$$F_3' = \cos \cdot \alpha \cdot F_3$$

Doubling the angle  $\alpha$  is equal to the  $\beta_2$ .  $\beta_2$  is the total angle of rotation of large cog gear required to length equal 40mm to shift lever controlling the output section A5 system.

If the angle  $\beta_2$  multiplying by gear ratio  $i=6$  we get the value of the angle  $\beta_1$  which expresses by how large an angle will shoot small gear which is connected with the engine. Angle  $\beta_1$  must be less than 180 degrees, because this value

is the maximum displacement of the servomotor. In this proposal is calculated the value of the angle  $\beta_1 = 173.7^\circ$ .

Motor is rotating at speed of 60 °/0.13sec. then the time  $t$  required to change the nozzle exit section of the  $A_{5min}$  to  $A_{5max}$  is calculated by the formula:

$$\frac{t}{\beta_1} = \frac{0,13}{60}$$

$$t = \frac{\beta_1 \cdot 0,13}{60}$$

$$t = 0,3764 \text{ s}$$

The results of the time, deflections and force came out in the required values as i preddict, however if we consider that the force required to operate system will output a maximum of 20 kg.

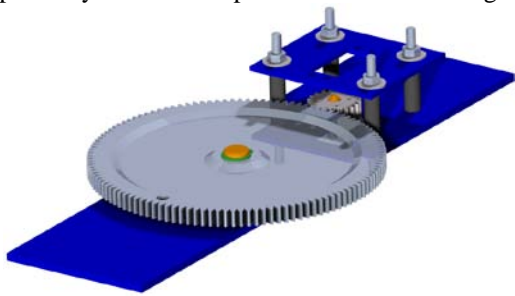


Fig. 5 Construction for the control of outlet nozzle by servo help

When you try to control the system output it was found that the power to change cross section is considerably higher and leader of this thesis increased value from 20 kg to 40 kg.

Ignorance of the necessary force to control the outlet nozzles is because to the nozzle exit (Fig. 1) is no technical documentation.

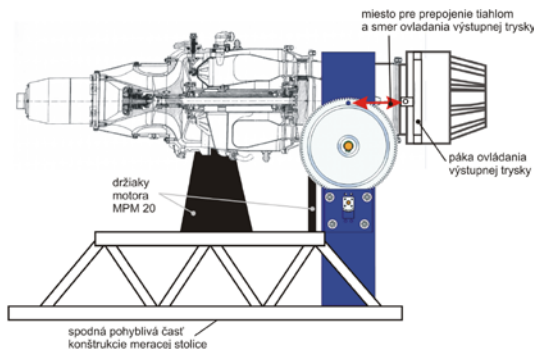


Fig. 6 Illustration of the location of the construction for controlling the output using the servo

For the use of that construction I design to use servomotor from PEGASUS labeled PA-R-340-9. The proposed servo control method has the same principle as described above servo HV DS8921.

Parameters:

- Constant torque of 10 Nm,
- Max. torque 17.5 Nm,
- Range of supply voltage  $U = 18$  to  $32$  V,
- Working angle of  $\pm 90^\circ$ ,
- Rotation speed  $230^\circ / 1 \text{ sec.}$

The above calculation of  $F_{3'}$  in the extreme position will be 726.184 N. The total time  $t$ , needed to change the cross section from  $A_{5max}$  to  $A_{5min}$  will be 0.76 sec..



Fig. 7 Servo PA-R-340-9

The advantage of the controlling would be the condition of the shortest duration and the possibility of continuous controlling and positioning servo at range from  $0^\circ$  to  $90^\circ$  right and left also.

The advantage of using a wheeled structure with servo is that the servo power is used in its entirety steering.

### 3.2 Controlling of electromotor MP-100 M

Given the electric MP-100M performs rod movement forward and backward.

Parameters:

- Namely - 100 kg,
- Maximum - 150 kg,
- Static - 400 kg,
- Power supply -  $U = 27 \text{ V}$ ,
- Current -  $I = 2 \text{ A}$ ,
- Speed - 2.29 to 3.1 (mm / s)
- The working stroke of - 10-80 mm.

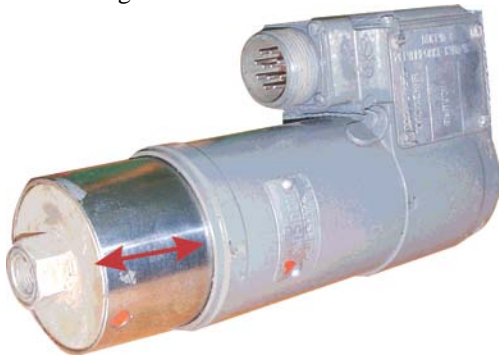


Fig. 8 Electric MP-100M

To use the MP-100M, I thought to speed up his movement by one lever. Conversion using a single lever showed that the engine does not meet the recruitments.

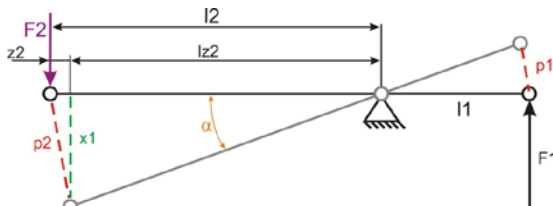


Fig. 9 Graphically outline of solutions to control the outlet nozzle by lever for MP-100M

$F_1$  is the force of electric engine.

The calculation procedure consists of:

$$Mk_1 = Mk_2$$

$$F_1 \cdot l_1 = F_2 \cdot l_2$$

One variant is that levers will be long  $l_1 = 30 \text{ mm}$  and  $l_2 = 80 \text{ mm}$ , then  $F_2 = 56.25 \text{ kg}$ , but the overall movement time will be 6.5 sec.. In this case, time and power directly dependent on each other, increases force  $F_2$  also increases the time needed to scroll.

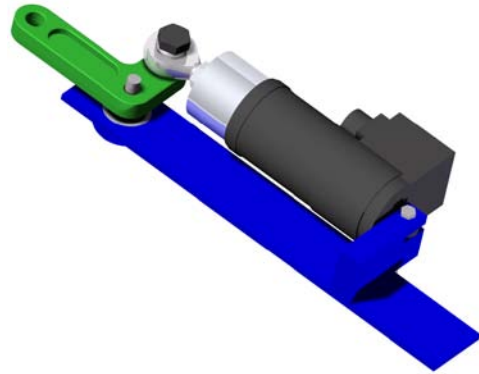


Fig. 10 Construction of controlling the output system using MP-100M and levers

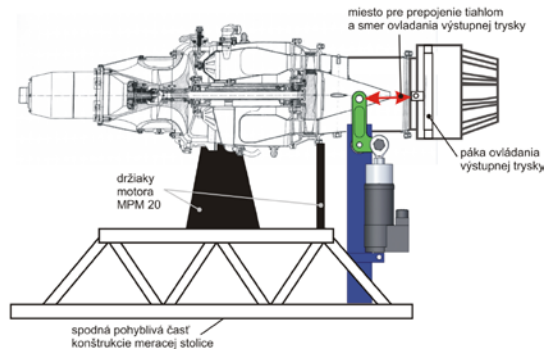


Fig. 11 Illustration of the location of the construction of the controlling system output using MP-100M and levers

## 4 CREATING A MATHEMATICAL MODEL OF MPM-20 ENGINE WITH ONE DEGREE OF FREEDOM AND IT'S VERIFICATION

Creating a mathematical model is based on one degree of freedom, where regulation is section of nozzle exit.

Based on the measured data in the test engine, the transient characteristic was created of Fig.12 - graph of dependence of variability of speed from change of the output section of the  $A_{5\min}$  to  $A_{5\max}$  at constant supply of fuel, where the x-axis represents time  $t$ , and y-axis is the rounds  $n$ . During the measurement, a change of rounds happened from  $n_{\min} = 47,850 \text{ (rpm}^{-1}\text{)}$ , to  $n_{\max} = 48,750 \text{ (rpm}^{-1}\text{)}$ .

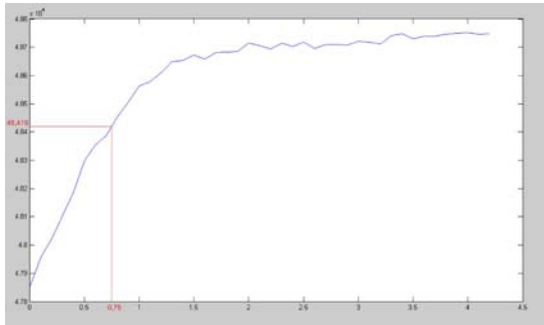


Fig. 12 The transfer characteristic of variable rounds by varying the output section of the  $A_{5min}$  to  $A_{5max}$  at constant fuel.

To determine the mathematical model of the engine MPM-20 was determined from the measured values gain of  $k_p$  and time constant  $T_p$ , which characterizes the transition story of rounds.

After determining the values of  $T_p$  and  $k_p A_5$  using MATLAB, I give the transition fig. 12 simulate the application through the SIMULINK block diagram in Fig. 13. The numerator is the value of  $k_p = 0.0293$ , and the denominator is the value  $T_p = 0.75$ .

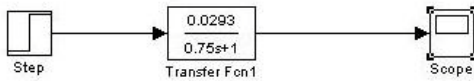


Fig. 13 Block diagram of the transmission functionality in MATLAB Simulink

The result of transient simulation plot is shown in Fig. 14, where the x-axis represents time and y axis the relative change in speed.

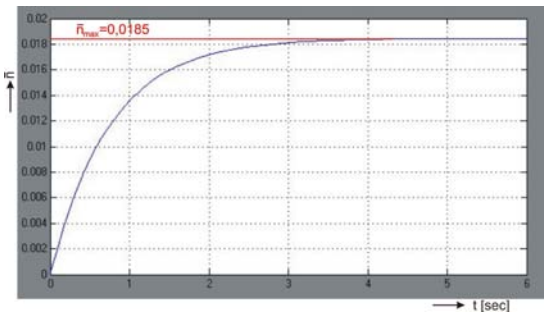


Fig. 14 The ideal transition of proportional variable rounds for sudden change of  $A_{5min}$  to  $A_{5max}$

Consolidating the process of value  $n_{max} = 0.0185$  means that the rounds has been reached  $n_{max} = 48750 \text{ rpm}^{-1}$ .

#### 4.1 Verification of the model engine MPM-20

Data of change rounds dependences on the change of cross section were measured manually by controlling the nozzle exit section. Due to security was made only one measurement to reliably determine the mathematical model and for its verification completely is not adequate. Used output system has a bug in its own construction, because the influence of exposure to high temperatures is an exit gas goes to temperatured change of materials of nozzle segments, causing unwanted change in the output section, and thus increase the rounds without moving the lever. It would therefore be appropriate to obtain a more accurate mathematical model and its verification, an adaptation of the nozzle or to construct new ones.

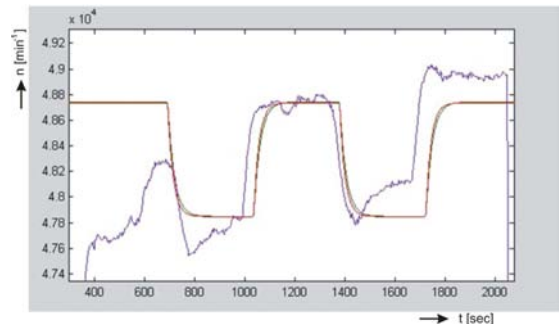


Fig. 15 Verification of the mathematical model of the engine MPM-20

At Fig. 15 we can see a comparison of simulation of transient processes of change of rounds with the measured data to the engine. The red curve is a simulation using function of 1st rad in Fig. 13 green curve represents the simulation using the method of gradual integration with the transfer function of 2nd order:

$$F(s) = \frac{75014}{0,0054s^2 + 0,6169s + 1}$$

#### 5 CONCLUSION

In thesis the design of controlling of change of cross section of the outlet nozzle, by

support of different power and mechanisms that serve to the use of force and motion orientation engine to change the output section in a relatively short time. Neither of the engine which leader of the thesis gave me was not suitable for the implementation of controlling system changes the output section. For functional operation, I proposed servo engine PA-R-340-9.

After installing the system output variable nozzle output values were measured by manual controlling of lever controled the outlet nozzle and the measurement was made. We compared measured values of changes rounds of engine with value simulations. The result of simulation using the first transfer function was significantly different from the simulation using the method of gradual integration, which was used for the transfer function of second transfer. These simulations, however, had significant deviations (about  $200 \text{ rpm}^{-1}$ ) from the actual measured values, mainly due to thermal change of material of outlet nozzle. The nozzle would be appropriate to modify or construct a completely new one.

#### ACKNOWLEDGMENT

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